# **EE365: Shortest Path Example**

#### Stochastic shortest path example



- ightharpoonup chain of n=100 nodes
- ightharpoonup move from node 10 to node 90 in T=100 steps
- ▶ can move forward one node, move backward one node, or stay put
- $\blacktriangleright$  at each time step, lightning strikes with probability 0.3
- ightharpoonup usually zero cost to move, unless lightning strikes, then cost at time t is
  - ightharpoonup t to move right
  - ightharpoonup -50 to move left
- minimize total expected cost

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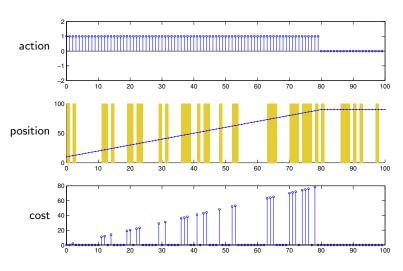
# Information patterns

#### three different information patterns:

- 1. open loop: only know probability of lightning strike
- 2. current: at each time, know whether lightning is striking now
- 3. prescient: know times of all future lightning strikes

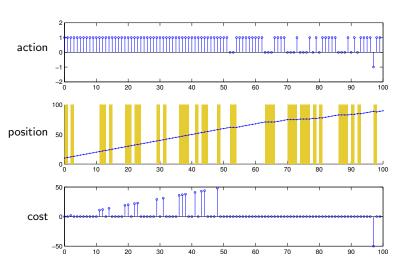
# Open loop

lightning strikes, in yellow. Total cost =1283



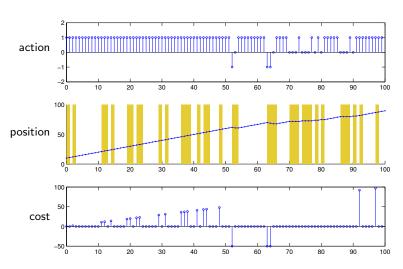
# **Prescient**

Total cost = 420

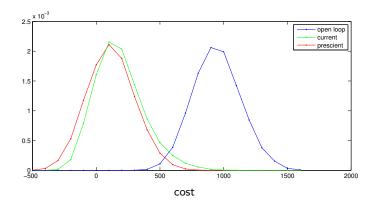


# Current

 $\mathsf{Total}\ \mathsf{cost} = 509$ 



#### Cost distributions



- ▶ cost distributions for each information pattern
- ▶ clearly shows value of information, recourse

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